

Math 150 Ch. 4 Review

1. Antiderivatives - guess and check (by taking deriv.)
 $\int x^n dx = \frac{1}{n+1} x^{n+1} + c$ Know Trig \int 's

2. Σ notation, Sum Arithmetic $S = \frac{(1^{st} + last) \# terms}{2}$

Calculator Sums

\approx Areas using inscribed, circumscribed, midpoint rectangles.

3. Definite \int : $\lim_{n \rightarrow \infty} \sum_{i=1}^n f(c_i) \Delta x$ or $\lim_{\|\Delta\| \rightarrow 0} f(c_i) \Delta x_i$
 $= \int_a^b f(x) dx$

Know what the pieces in the Riemann sums above represent

Properties:

1) $\int_a^b f(x) dx = \text{Area}$ iff $f(x) \geq 0$

2) $\int_a^a f(x) dx = 0$

3) $\int_a^b f(x) dx = -\int_b^a f(x) dx$

4) $\int_a^b f(x) dx + \int_b^c f(x) dx = \int_a^c f(x) dx$

Integration by areas of known shapes

4. $\int_a^b f(x) dx = F(b) - F(a)$ where $F'(x) = f(x)$

MVT \int : $f(c) = \frac{1}{b-a} \int_a^b f(x) dx$ where $f(c) = \text{average value}$

If $F(x) = \int_{g(x)}^{h(x)} f(t) dt \Rightarrow F'(x) = h'(x)f(h(x)) - g'(x)f(g(x))$

\int by Substitution: Try $u = \text{thing to a power}$
 $u = \text{angle of trig function}$

Article Problems